

Using maps of city analogues to display and interpret climate change scenarios and their uncertainty*

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Abstract

We describe a method to represent the results of climate simulation models with spatial analogues. An analogue to a city A is a city B whose climate today corresponds to A's simulated future climate. Climates were characterized and compared non-parametrically, using the 30-years distribution of three indicators: Aridity Index, Heating Degree Days and Cooling Degree Days. The level of correspondence (i.e. strength of analogy) was evaluated statistically with the two-samples Kolmogorov-Smirnov test, generalized to 3 dimensions. We looked at the climate of 12 European cities at the end of the 20th century under an A2 climate change scenario. We used two datasets produced with high-resolution regional climate simulation models from the Hadley Centre and Meteo France. As expected from the modelled warming in local climate, analogues were found in warmer regions, mostly at more southerly latitudes within Europe, although much model and scenario uncertainty remains. Climate analogues provide an intuitive way to show the possible effects of climate change on urban areas, offering a holistic approach to think about how cities might adapt to different climates. Evidence of its communication value comes from the reuse of our maps in teaching and in several European mass-media.

1 Introduction

According to the United Nations, Department of Economic and Social affairs (2004), the majority of humankind is now living in urban areas. Especially the European population is predominantly city-dwelling, with 65.6% residing in urban areas in 1975, a number that rose to 71.7 % at the turn of the century and is prospected to reach 78.3% by 2030. In cities, weather patterns interact with the socio-economic structures directly and indirectly in many uncounted and mostly unaccountable ways. Elevated temperatures, particularly during extremes like the 2003 and 2006 summers, have shown the heavy strain on and need for adaptation of sanitary systems, production strategies (above all in construction), power supply systems, living conditions and

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so forth. The full extent of the impact of such climatic events on society could not be predicted but only analyzed in retrospect. However, due to adaptation and evolution of societies, even the recurrence of an identical extreme events would most likely have different consequences. An integrated assessment of the impact of future climate change on urban areas would require a systematic consideration of a large number of heavily interwoven urban attributes which affect the adaptation process, such as architectural styles, transport infrastructure and cultural lifestyles. Defining a convincing reference scenario under these conditions, together with a consistent vision of economic and cultural drivers of the adaptation process, is a daunting task. Predicting the consequences of climate change on human settlements accurately seems not feasible at this point.

Hallegatte et al. (2007) suggested an alternative, holistic approach to the assessment of socio-economic consequences of climate change. The authors proposed to search and evaluate current analogues of the future climate of urban areas. In order to think about how city A will be in the future, they suggest to look at how city B is in the present, whose current climate is like the simulated future climate of A. Although this method might omit or oversimplify other potentially important aspects of comparability between such two locations, it does circumvents the obstacle of having to theorize adaptation to the consequences of climate change.

The concept of spatial analogues is not new though. The use of analogue regions to assess climate change impacts on agriculture has been suggested already by Parry and Carter (1989) and was previously used by Darwin et al. (1995) as well as Mendelsohn and Dinar (1999). Such spatial analogues have also been exploited for a variety of other applications such as, for example, the projection of vegetation composition, snow conditions for skiing and avalanche risk (Mearns et al., 2001). This contribution extends and improves the approach initially proposed by Hallegatte et al. (2007), by presenting a statistical methodology to identify climate analogues. This method is generally applicable to high spatial resolution climate simulation models, is computationally light, and does not need any hand tuning.

There are two key methodological choices for a climate analogue method. The first is which climate indicators to use. As the next section discusses, climates are characterized here using three indicators: Aridity Index, Heating Degree Days and Cooling Degree Days. The second choice is how to compare climates statistically. As discussed in Section 3, the proposed method does not rely on averages or on parametric tests, but applies the 3-dimensional two-samples Kolmogorov-Smirnov test directly to the 30-years distribution of the indicators. Section 4 demonstrates applicability by computing analogues for 12 large European cities using data from two high-resolution regional climate simulation models from the Hadley Centre and Meteo France. In the concluding section 5, we discuss the method's limits, potential improvements, and communication value in several European mass-media channels.

Three technical appendices describe respectively A) the parameterization of the K-S test, based on Monte-Carlo simulations in the literature, B) more detailed results on the comparison between using 3 indicators versus only 2, and C) the difference between p-value maps versus maps of the KS statistic, that we use preferentially because they offer a better visual contrast.

2 Characterizing climate with indicators

2.1 Indicators

Climate can be defined as the weather conditions in a certain geographical area averaged over a long period of time. A more quantitative definition is needed for a computer-based method. A well accepted approach to characterize climates is to select a few aggregate indicators quantifying the most relevant attributes such as measures of seasonal and annual warmth or cold, accumulated wetness/dryness, solar radiation, atmospheric humidity, etc. Many climate indicators exist, as climates can be defined in different ways for different purposes. For example, in agriculture the total annual evapotranspiration is an important indicator for plant growth, whereas in tourism the total number of rainy days might be of primary interest instead. The literature suggests that general-purpose characterizations of climates, such as the Köppen classification, tend to include at least one indicator related to temperature (or energy) and one indicator related to moisture (or water). The popularity of the Holdridge (1947) Life Zone system shows that three indicators are sufficient to define a useful classification of climates (in this classification, the indicators are temperature, precipitation and evaporation, but the zones are represented on a two dimensional triangle because the third indicator is a combination of the first two).

In order to characterize climate from the point of view of its impact on cities and urban life, we considered the combination of the following three climate indicators: annual Aridity Index, annual Heating Degree Days and annual Cooling Degree Days. The annual Aridity Index represents a key factor defining water deficit. This index is widely used in the categorization of climate types, and water stress is expected to be a key social impact of climate change. The Heating and Cooling Degree Days measure accumulated temperature and are known to correlate well with the energy demand for heating and air conditioning, respectively. They are used in financial markets to settle the price of weather derivatives and futures (e.g. van Asseldonk, 2003), or to estimate a building's or a city's energy needs. Similar measures of accumulated temperature are also used in agriculture (Monteith, 1981), for example the Effective Temperature Sum (ETS) used by Fronzek and Carter (2007) as an indicator of thermal suitability for crop development.

Although capturing additional aspects of climate or investigating selected features or particular subsystems of urban areas might require additional indicators, there is a certain trade-off between the exhaustive description of a local climate and the practical ability to identify analogues of that climate. We believe that the combination of these three indicators provides a sufficient description of a city's climate to assess the impact of climatic change on urban areas, so we define climate for this study as the 30-year joint three-way distribution of the Aridity Index, Heating Degree Days and Cooling Degree Days. In order to statistically compare climatic (dis-) similarities between different times and places, we assume stationarity, as if the 30 years were drawn from the same unchanging distribution. No assumption is made on the shape of this distribution. The three indicators are defined in principle from daily data, but monthly mean temperature and precipitation data are more readily available. As we show next, the indicators can be computed to a good approximation from monthly data.

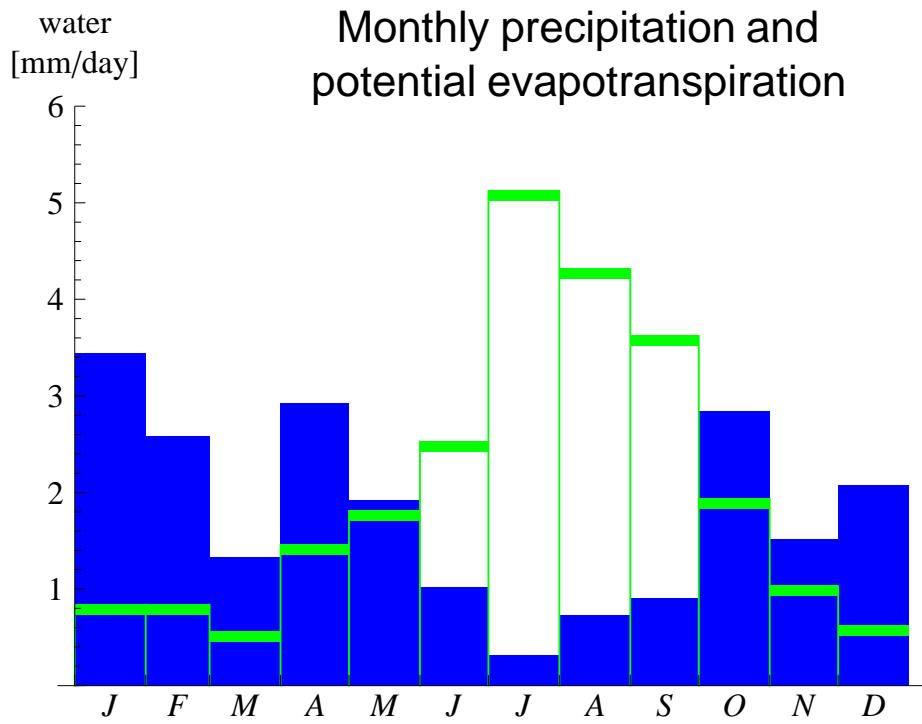


Figure 1: Mean monthly precipitation (blue bars) and potential evapotranspiration (green bars) of the simulated climate of Paris in 2071 (HadRM3H model, single grid box). Absolute aridity is the area above the precipitation and below evapotranspiration bars of the deficient months (hollow rectangles). It is divided by total evapotranspiration of the deficient months to get the aridity index.

2.2 Aridity

Aridity describes the availability of water that plants can use. It is a fundamental indicator for a climate's vegetation, likely to change significantly in a changing climate. There are several variants of an aridity index available in the literature: absolute or relative, aridity or humidity. For the purpose of describing climates statistically they are largely equivalent, so we settled on the classical Aridity Index AI as defined by Thornthwaite (1948) (see Figure 1) and restated below:

In any given month, the water deficit is the difference between the monthly potential evapotranspiration e and the precipitation p which sums up for all water deficient months of a year to the annual water deficit. The annual Aridity Index is defined relative to the total potential evapotranspiration of the deficient months:

$$AI = 100 \frac{\sum_{i=1}^{12} \delta_i (e_i - p_i)}{\sum_{i=1}^{12} \delta_i e_i} \begin{cases} \delta_i = 1 & \text{if } e_i > p_i \\ \delta_i = 0 & \text{if } e_i \leq p_i \end{cases} \quad (1)$$

Thornthwaite (1948) also provides an empirically derived method for closely estimating the monthly potential evapotranspiration e of a standard month of 30 days in cm from the mean monthly temperature t_i in $^{\circ}C$:

$$e_i = 1.6 \left(\frac{10 t_i}{I} \right)^a ; t_i > 0^{\circ}C \quad (2)$$

with

$$I = \sum_{i=1}^{12} \left(\frac{t_i}{5} \right)^{1.514} ; t_i > 0^{\circ}C \quad (3)$$

$$a = 0.000000675I^3 + 0.0000771I^2 + 0.01792I + 0.49239 \quad (4)$$

As the days in a month vary and the number of hours of sunshine per day depend on the seasons and the latitude, Thornthwaite (1948) also introduced an adjustment factor for the above calculated unadjusted potential evapotranspiration. This method is also known to systematically underestimate the potential evapotranspiration in more arid regions and seasons as it was developed and parameterized for conditions in the USA (e.g. Deichmann and Eklundh, 1991). In the present work, we neglected these adjustments but follow-up studies should investigate this aspect.

2.3 Cooling and heating degree days

Heating and cooling degree days (HDD and CDD , see Figure 2) can be seen as measures of heating and air conditioning needs, respectively. They are based on the simple idea that heaters (or air conditioners) are turned on when the daily mean temperature t_n drops below (or rises above) a reference temperature b . We will use $b = 18^{\circ}C$, as mentioned in World Meteorological Organization (1983, p. 1B.5). There is empirical evidence that it is the center of the comfort interval outside of which the energy demand increases (Mitchell et al., 1974; Valor and Caselles, 2001). The precise value of b is not critical to our method, as the indexes with different b are well correlated. Other reference values include 65F, or 18.33 $^{\circ}C$, used on the Chicago market for weather derivatives, and 15.5 $^{\circ}C$ used traditionally in the UK. These indicators' relevance for the

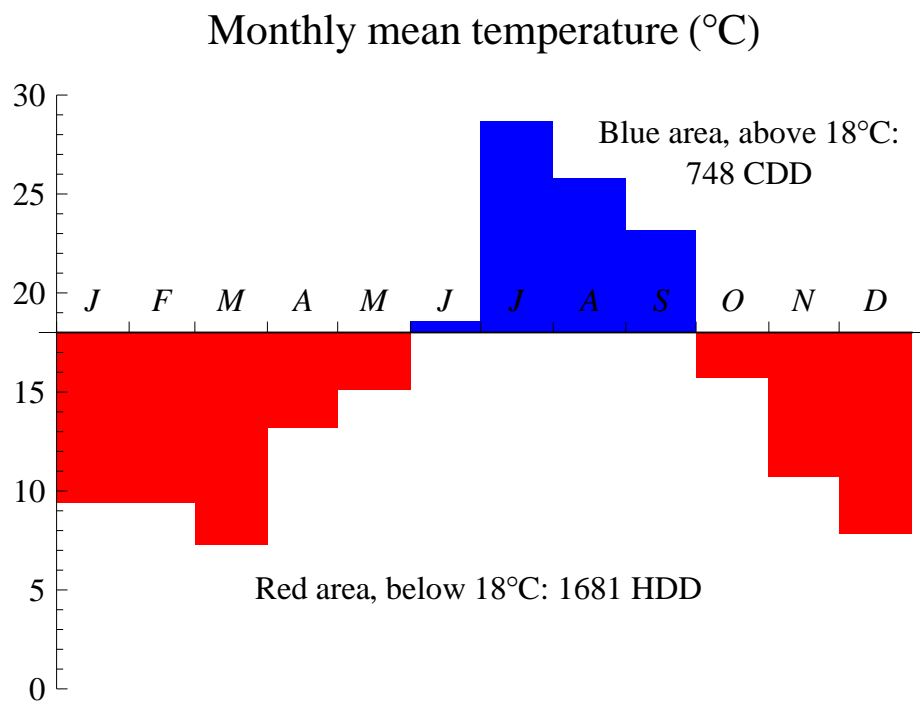


Figure 2: Temperature simulation for Paris in 2071 (HadRM3H model). Cooling Degree Days (CDD) correspond to the area above the 18°C line (blue area). Heating Degree Days (HDD) correspond to the area below the 18°C line (red area). The CDD and HDD for each month are empirical approximations based on monthly mean temperatures.

climate change issue is twofold. On one hand, changes in their distributions are an expected important impact of climate change. And on the other hand, they also matter for mitigation, since degree days empirically characterize households' energy consumption very well. Mathematically, annual heating and cooling degree days are defined as follows:

$$HDD = \sum_{n=1}^{365} \delta_n (b - t_n) \begin{cases} \delta_n = 1 & \text{if } b > t_n \\ \delta_n = 0 & \text{if } b \leq t_n \end{cases} \quad (5)$$

$$CDD = \sum_{n=1}^{365} \delta_n (t_n - b) \begin{cases} \delta_n = 1 & \text{if } t_n > b \\ \delta_n = 0 & \text{if } t_n \leq b \end{cases} \quad (6)$$

Although based, by definition, on a daily difference to the base, by observing that the daily temperature distribution has a known shape, it is possible to estimate monthly degree days statistically from monthly temperature means, neglecting Schär et al. (2004)'s suggestion that climate change may alter this known shape. Thom (1954, 1966) proposed a method to calculate the monthly degree days above (CDD_m) or below (HDD_m) any base as follows:

$$HDD_m = N [l_{HDD}^*(+x_0) \sqrt{N} \sigma_m - (t_m - b)] \quad (7)$$

$$CDD_m = N [l_{CDD}^*(-x_0) \sqrt{N} \sigma_m + (t_m - b)] \quad (8)$$

where N is the month length in days, t_m the monthly mean temperature, σ_m the standard deviation of monthly average temperature (which was calculated in our case from the available average monthly temperatures over several years as available), $b=18^\circ\text{C}$ the base, and x_0 and $l_{HDD/CDD}^*$ the so-called truncation point and respective truncation coefficient, which are related empirically and calculated with an exponential approximation (Thom, 1966) as follows:

$$x_0 = \frac{b - t_m}{\sqrt{N} \sigma_m} \quad (9)$$

$$l_{HDD}^*(+x_0) = 0.34e^{-4.7x_0} - 0.15e^{-7.8x_0} \quad (10)$$

$$l_{CDD}^*(-x_0) = 0.34e^{-4.7x_0} - 0.15e^{-7.8x_0} + x_0 \quad (11)$$

This method only approximates the monthly HDD and CDD, but for European climatic conditions it provides a reasonable replacement estimate for calculations based on daily temperature.

3 A statistical measure of climatic similarity

3.1 The 1-Dimensional two sample Kolmogorov-Smirnov test

The Kolmogorov-Smirnov test is a commonly used and relatively simple non-parametric statistical test. It can be used to examine if a sample comes from a known distribution, or to examine if two samples come from the same unknown distribution. Our use is the latter: to compare climates from two different places and periods, using samples of 30 years. In its basic univariate case, the Kolmogorov-Smirnov statistic D is defined

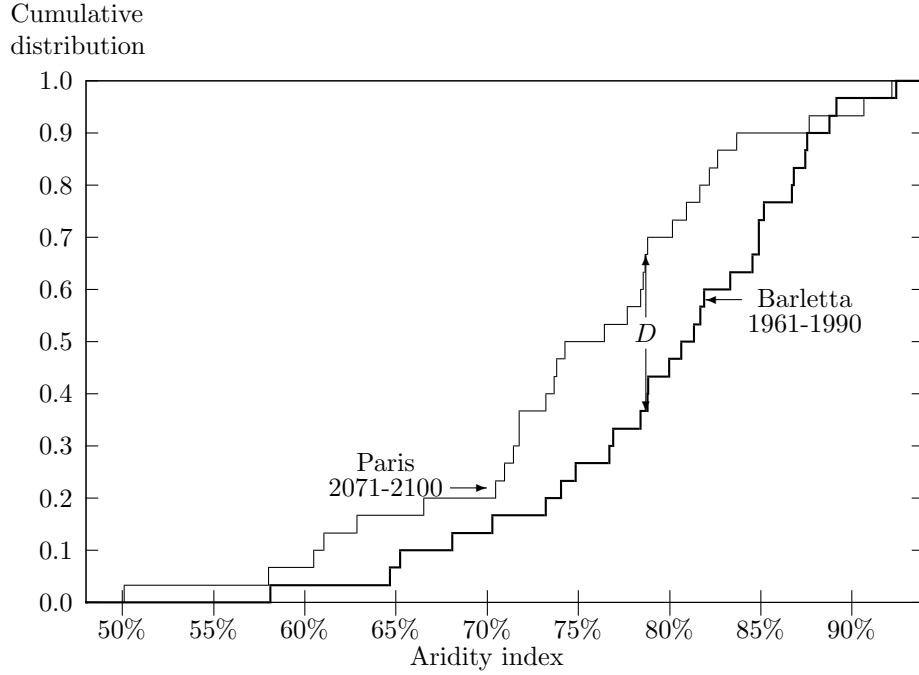


Figure 3: Cumulative Probability Distributions of the Aridity index for Paris (2071–2100) and the southern Italian city Barletta (1961–1990), data from HadRM3H model. The Kolmogorov-Smirnov statistic D is the maximum vertical distance between the two curves.

as the maximum vertical distance between the cumulative distribution functions of the two samples. This is illustrated in Figure 3 for the cumulative distribution of the 30 annual aridity indices of the climate of Paris from 2071 to 2100 and the climate of the southern Italian city Barletta from 1961 to 1990 respectively (aridity indices computed using the results of the HadRM3H model simulation.)

The basic idea of the test is the following. When one draws two samples of numbers according to a given probability distribution f , the cumulative distribution curves of the two samples will both tend to fall around the same PDF curve of f . Thus, if one cannot expect D to be exactly 0, one can expect it to be small. But when one draws two samples according to very distinct probability distributions, respectively f and g , the cumulative distribution curves of the two samples will tend to fall around the PDF curves of respectively f and g . If these curves are well apart, one can expect the statistic D to be close to 1. To illustrate with an extreme case, if numbers drawn according to f are known to lie within $[1, 2]$ and numbers drawn according to g are in $[3, 4]$, then certainly the distance will be 1.

The frequency distribution p of the K-S statistic D for two samples of 30 drawn from the same distribution f can be computed empirically to an adequate level of precision for application by using Monte-Carlo simulation. The key to the K-S test is that p does not depend on the shape of f itself. Thus, the K-S is non parametric, as very few assumptions need to be made on the unknown distribution: Fasano and Franceschini (1987) show that for the 2- and 3-dimensional case, only the correlation between the variables matter. Figure 4 displays the distribution according to the literature.

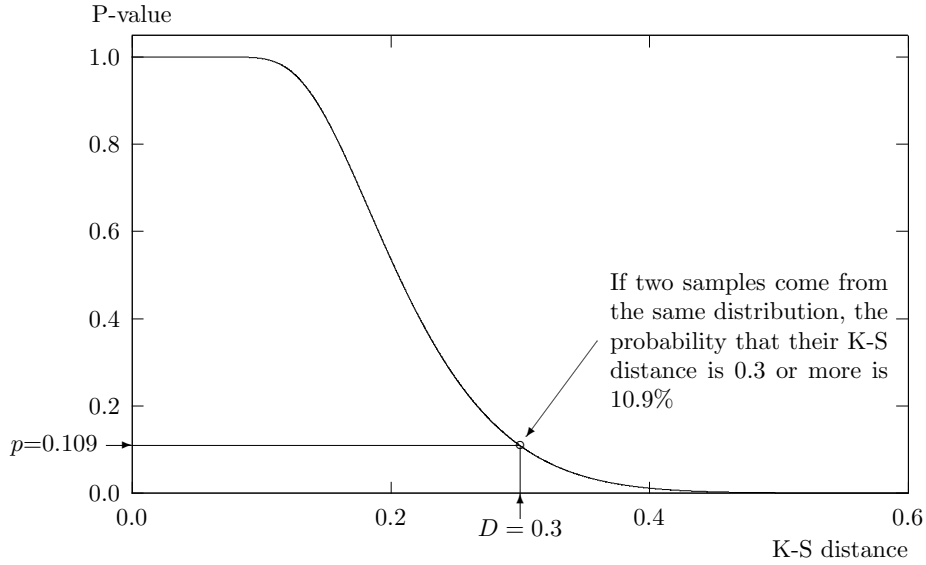


Figure 4: The p_{value} as a function of the K-S statistic D after Press et al. (1992). It measures on an absolute scale (between 0 and 1) how likely it is for two samples to be drawn from the same distribution i.e. in our case, how well the two climates, as described by the indicator, correspond.

The Kolmogorov-Smirnov distance D offers an absolute measure of similarity between two samples based on statistical theory. In technical language, the probability that two samples drawn from the same distribution have a K-S statistic at least as great as D is called the p -value. For example, the p -value of two identical samples ($D = 0$) is $p = 1$. When the p -value is small, there is reason to reject the hypothesis that the two samples come from the same distribution. On the contrary, the larger p , the more reason there is to believe (or accept the hypothesis) that the two samples were indeed drawn from the same distribution.

3.2 The 2-D and 3-D Kolmogorov-Smirnov test

The classical K-S test presented above deals with real-valued variables (i.e. is 1-dimensional). However, we characterize climates with three indicators, so we have to test the three-way joint probability distribution AI, HCC and CDD. Generalization is not trivial because in higher dimensions there is no obvious total ordering relation, so the notion of cumulative distribution is not immediately applicable. We used generalizations of the K-S test for two (Peacock, 1983) and three (Fasano and Franceschini, 1987) dimensions.

In the case of two-dimensional samples, each data point is a pair of numbers, such as (AI, CDD) for example. The approach of Peacock (1983) is best understood graphically, as illustrated in Figure 5 for the combination of annual Aridity Index and annual Cooling Degree Days over 30 years of simulated climate for Paris, from 2071 to 2100, and Barletta, Italy, from 1961 to 1990. It replaces the cumulative probability distribution with a description of the integrated probability in each of the 4 quadrants around a given *reference point* (x,y) of the sample. Practically, each data point of the sample is successively used as the reference point. For each such reference point, the relative

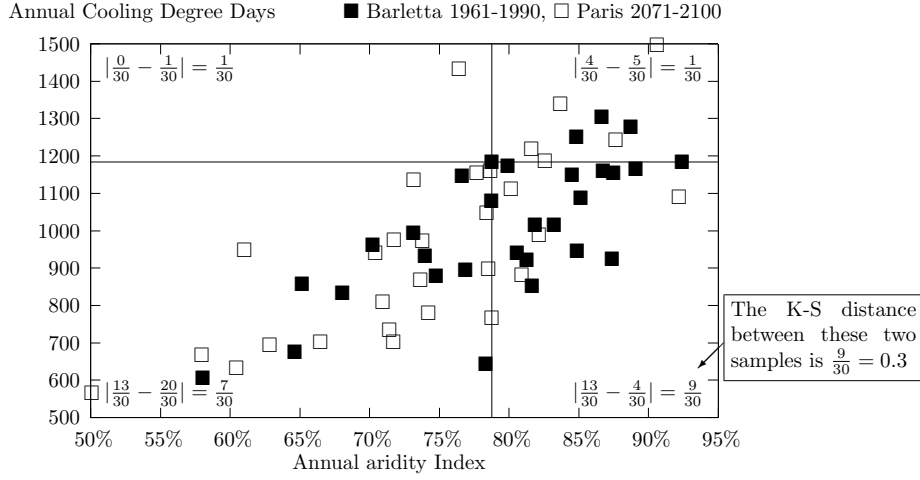


Figure 5: Spatial distribution of the combination of the two climate indicators annual Aridity Index and annual Cooling Degree Days from 30 years for Paris (2071–2100) and the southern Italian city Barletta (1961–1990), data from HadRM3H model. The Kolmogorov-Smirnov statistic D is the maximum difference of the integrated probabilities of the two distributions in the 4 quadrants around each data point. The figure displays this calculation with one data point as a reference, in which case the maximum difference is $9/30 = 0.3$ found in the forth quadrant. To find the maximum, the same calculation is performed for all data points, which yields the displayed difference of $9/30 = 0.3$ as absolute maximum.

frequencies for the two samples are calculated in each quadrant, as the ratio of the number of data points in the quadrant to the total number of data points. Finally, The K-S statistic D between two samples is the maximum difference of the relative frequencies in the 4 quadrants, when considering successively all data points as the reference point.

Generalizing the 2-dimensional version of the K-S statistic D to the 3-dimensional case is straightforward. Each data point is a triple, for example (AI, CDD, HDD). These data points can be seen as a cloud in 3-dimensional space. There are 8 octants in the space around each data point instead of 4 quadrants in the plane. The K-S statistic D between two sample distributions is taken as the maximum difference of the relative frequencies when considering the 8 octants around all data points.

For statistical testing, the translation of the K-S statistic D into the p_{value} in the multi-dimensional cases is based on the same Monte-Carlo methods as in the 1-dimensional case. Technically, given a distance D measured between two tested samples, the p_{value} is the probability that the K-S distance between two samples randomly drawn from the same distribution is greater than D . It describes how well the two samples are similar, or could come from the same probability distribution. In other terms, the p_{value} is the likelihood that the two samples are two realizations from the same probability distribution. In our case, it also means how well two climates, as described by multiple indicators, coincide. Technical details on the probability distributions used in the 2- and 3-dimensional cases are shown Appendix A.

3.3 Analogue Filtering, Selection and Visualization

The selection of the best current analogue to a city’s future climate amounts to searching for a local minimum in D . We used two additional filters.

First, only grid points in the model with a p_{value} greater than 0.5 were considered acceptable for further evaluation. Locations that reject the “same climate” hypothesis at a 50% confidence level were not acceptable. According to the usual practice of statistical testing at 95%, this is a quite low confidence level. But the purpose is not to test for all analogs, only to simplify further computations by filtering out a large fraction of grid cells. When no grid cell is acceptable, the search fails.

Second, we penalized narrow optima by applying a lowpass spatial filter before minimizing the D field. The filter combined the score of a cell with a 0.5 weight, with the score of its four cardinal neighbors located at plus or minus 0.5° latitude/longitude, using a 0.125 weight. Neighbors were obtained by interpolation when the datagrid made it necessary. The justification for this smoothing is heuristic. The analogue is meant to represent a climate to readers who have a fuzzy mental representation of European climates. This goal is better accomplished when the optimum is within a large region of good analogues.

The optimum was found using exhaustive search, as this is nonconvex optimization with a finite, computationally tractable number of points (one per grid cell). Compared to Hallegatte et al. (2007), no further heuristic arbitration between candidate optima was needed. The smallest smoothed K-S statistic at an acceptable location was considered the best analogue. It was then possible to name the analogue according to the closest meteorological station or city.

Based on this method, two kinds of maps were drawn. The first kind is the “climate analogues quality” map, shown in Figure 7. It shows where one can currently find the future climate of a given city, by mapping the K-S statistic D on a regular grid of Europe, at the resolution of the original dataset. We used interpolation when the original dataset was not on a rectangular grid. Appendix C discusses why we choose to display D instead of the p -value. This kind of map allows the reader to check visually the quality of the “best” analogue, which is necessary since it involves nonconvex local minimization.

A second kind of map is the “climate relocation” map. It is obtained by selecting a set of cities, and displaying where their best analogue lies on a common map of Europe (see Figure 8). These maps communicate the directions and order of magnitude of climate changes expected over the course of the century. In order to convey the uncertainty related to climate simulations, it is important to always show several such maps obtained by different models or emissions scenarios.

4 Application

4.1 Data and implementation

The method was implemented in Fortran, using `g77` with the GrADS, NetCDF and CDO libraries. For city coordinates, we took the list of stations from the Global Historical Climatology Network 2 dataset. The code uses resources from Press et al. (1986), is released under the GPL and available from the CIRED web site (<http://www.centre-cired.fr>). It can be parameterized to examine most large cities in Europe. For this paper, we examined analogues for 12 large European cities: Athens,

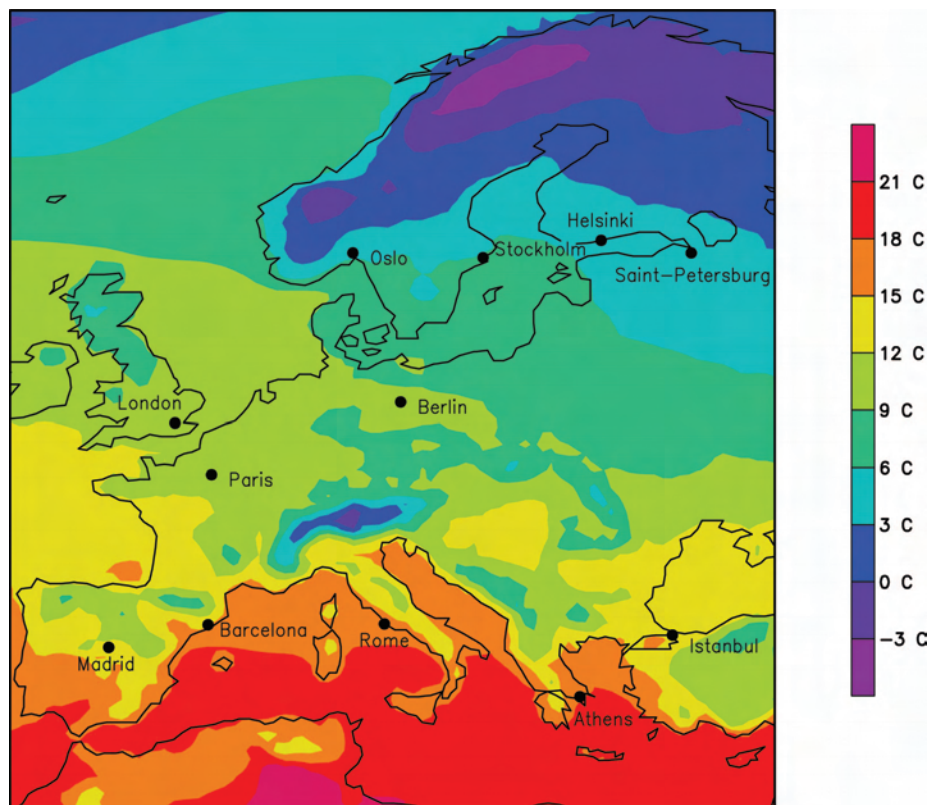


Figure 6: Cities examined in this study, displayed on a mean temperature background from the HadRM3H control run (1961-1990) for a basic impression of relative temperatures.

Barcelona, Berlin, Helsinki, Istanbul, London, Madrid, Oslo, Paris, Rome, Saint-Petersburg and Stockholm, as shown in Figure 6.

The key inputs needed are regional 2D fields of mean monthly surface temperatures and precipitations. Data should be at relatively high spatial resolution, about 50 km grid. It should cover two 30 years spans, in order to compare the present and the future climates. Finally, it should cover a reasonably wide latitudinal zone, since warmer climates are to be found southward.

We used two climate simulation datasets from models of the PRUDENCE project (from ensemble 1 simulations described in Christensen and Christensen (2007)). One dataset is the *DE6* run of the ARPEGE-Climate model from CNRM/Météo-France. This is a global circulation model with a variable horizontal resolution of up to 50km in Europe. This atmospheric model was forced by sea surface temperature of the HadCM3 A2 model. The other dataset is the *ackda* run of the HadRM3H model from the Hadley Centre, a regional model with a 50-km resolution, forced by the global circulation model HadAM3H A2. Both models simulate a warming over Europe with an increase in precipitation in the North and a strong drying over the Mediterranean. In these datasets, the HadRM3H model simulates a stronger global warming response than the ARPEGE model, but both are within the range of the typical literature values according to the PRUDENCE intermodel comparisons. They both provided monthly mean temperatures and precipitations over 30 years in the present climate (control run, 1961–1990) and the projected future climate (2071–2100).

4.2 Comparing two versus three indicators

We compared empirically the results of the method as described above, based on a 3-dimensional K-S test using three indicators (Aridity Index and both Degree Days), with a simplified version using only two indicators (and a 2-dimensional K-S test). There are three possible ways to pick two indicators out of three, but theoretically it is hardly defensible to throw away the Aridity Index and keep only the two temperature-based indicators. This is why we tested only (AI, HDD) and (AI, CDD).

Figure 7, based on the HadRM3H model simulation, compares the climate analogues maps computed with three and two indicators for Paris and Saint-Petersburg. Logically, it can be seen that the first map in each row is like the fuzzy intersection of the second and third map.

The analogue location selected by the 3D test is also relatively good when tested with the 2-dimensional criteria, whereas the converse is not necessarily true. For example, for Paris the testing method with all 3 indicators found the best climate analogue close to the small Spanish city of Badajoz at the Spanish-Portuguese border with a p_{value} of 90%. This location also evaluates to a p_{value} of 100% in the 2-dimensional test with Aridity Index and Heating Degree Days as well as a p_{value} of 75% in the 2-dimensional test with Aridity Index and Cooling Degree Days.

Also, the best analogue with (AI, CDD) may be a poor one when seen with (AI, HDD) or vice versa. In the same example, the locations of the best analogues found by either of the 2-dimensional tests (for the test with Aridity Index and HDD located in the Black Sea and for the test with Aridity Index and CDD close to the Spanish city of Ciudad-Real) evaluate to a p_{value} of 0% in the other test. This example is representative of all 12 examined cities (see Appendix B).

In short, the results are not only theoretically but also empirically more satisfying using three indicators, and since the supplementary computational cost is modest, there is no reason to use just two. We did not look beyond three, but in some case this may

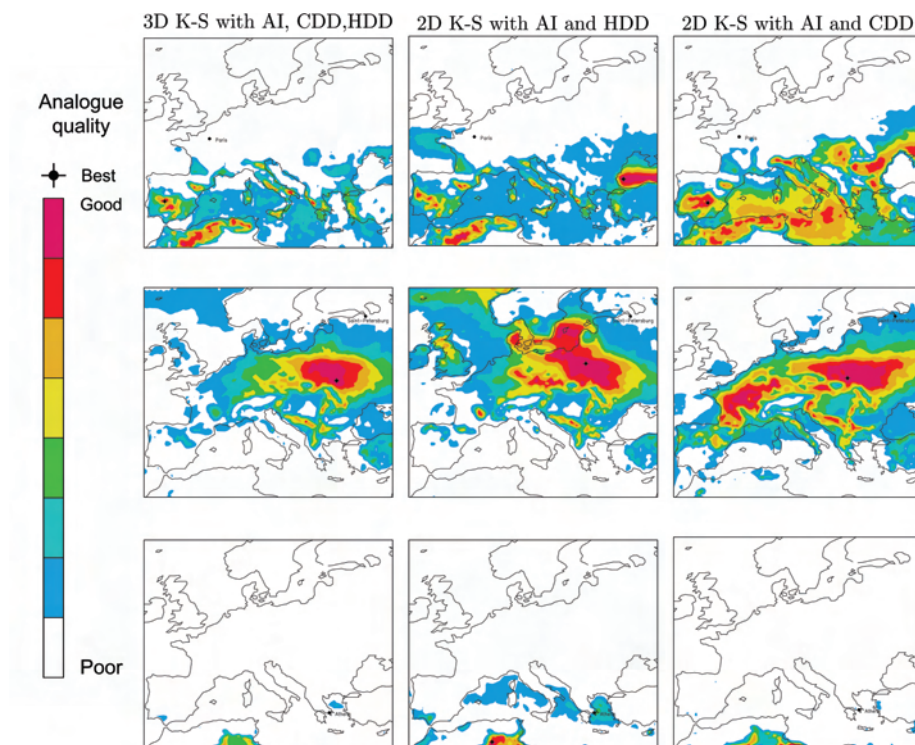


Figure 7: Comparison of the 3-dimensional K-S statistic results (with Aridity Index, HDD and CDD) and the two 2-dimensional K-S statistic results (with Aridity Index and HDD/CDD respectively) for Paris, Saint-Petersburg and Athens. Respective city's actual location indicated on each map along with the best climate analogue (if existent). (HadRM3H model simulation)

be useful, because in many cases there are several analogues approximately as good as each other. For example, all dark red areas in Figure 7 for cities like Paris and Saint-Petersburg. Possible extensions, to name only a few, would be, for example, an indicator expressing seasonality to account for urban adaptation to seasonal variations, an indicator reflecting the effect of elevation in order to consider climatic particularities at different altitudes, or an indicator capturing water surplus to account for structural adaptations needed to combat extreme events linked to excess water such as flooding, landslides and erosion.

4.3 Climate relocation maps

Variability in the prediction of future climate arising from the stochastic nature of climatic processes is accounted for, but deeper uncertainties remain (Ha-Duong et al., 2007). Climate relocation maps can be used to compare the output of climate models and to better understand the differences between climate change simulations. Figure 8 compares the analogues found for the different datasets: the ARPEGE and HadRM3H models projecting global warming. Figure 6 was the reference map of actual locations of the examined 12 cities in Europe.

No good analogues were found for Athens in either model. For HadRM3H, Barcelona

has an analogue near the town of Ouezzane in northern Morocco and Rome has an analogue on the southern coast of Turkey with Nicosia (the capital of Cyprus) being the closest analogue city. Neither has a good analogue for ARPEGE. Madrid by contrast has no good analogue for the HadRM3H simulation and Biskra in Algeria for ARPEGE. Berlin, London, Paris and Istanbul have good analogues near Chlef (Algeria), Vila Real (Portugal), Badajoz (Spain) and Kamaran (Turkey) respectively for HadRM3H, and Campobasso (Italy), Nantes (France), Vieste Aero near Rome (Italy) and Moron de la Frontera in Andalusia (Spain) for ARPEGE. Helsinki, Oslo, Stockholm and Saint-Petersburg have good analogues near Sandomierz (Poland), Teruel (Spain), Soria (Spain) and Ternopol (Ukraine) respectively for HadRM3H, and Banja Luka (Bosnia and Herzegovina), Klodzko (Poland), Lindenberg (Germany) and Rovno (Ukraine) for ARPEGE.

Comparing the analogues found in the case of the ARPEGE and HadRM3H models, which are two leading climate simulation models, give an impression of the extent of uncertainty in climate change prediction for Europe. Despite the differences, however, both models agree in showing a clear drift towards warmer regions in the climate analogues. This supports the expected effect of global warming on European local climates towards the end of the 21st century, under the A2 greenhouse gas emission scenario. It has to be noted however, that this simple two model comparison provides only a limited impression of the uncertainty. Future studies should investigate multi-model and multi-scenario comparisons to further assess the applicability of the method for the visualization of uncertainty and possibly the identification of different sources of uncertainty. Also, uncertainties such as those arising from biases in the control runs representing present-day climate should be taken into consideration.

5 Conclusions

We described a method to analyze the results of climate simulation models, improving on Hallegatte et al. (2007). It is based on the concept of climate analogues, i.e. finding a City B whose present climate statistically corresponds to the simulated future climate of an evaluated City A. This provides an intuitive visualization of climate change effects on urban areas, by replacing the change of climate (in time) with a change of a city's location (in space). Through the use of several models and scenarios, this approach also clarifies the extent of the uncertainty in climatic change predictions, and in their effects on urban areas.

Climates were characterized using three annual indicators: Aridity Index, Heating Degree Days and Cooling Degree Days. These indicators can readily be computed from monthly precipitation and temperature datasets. To compare climates, we compared 30-years time series of these indicators using the two sample three-dimensional Kolmogorov-Smirnov tests. We found that using three instead of only two climate indicators provided a more satisfying analogue selection, at the cost of a moderate increase in computational complexity.

The limitations of the approach lie primarily with the assumption of climate stationarity and the interpretation of a density map by its maximum alone (the *best* analogue). Also, analogues found might be physically implausible such as locations in the Mediterranean or Black Sea, and the selection of climate indicators focused primarily on precipitation and temperature derived characteristic could possibly obliterate important differences between a location and its analogue such as topography, length of day, level of economic development, etc.

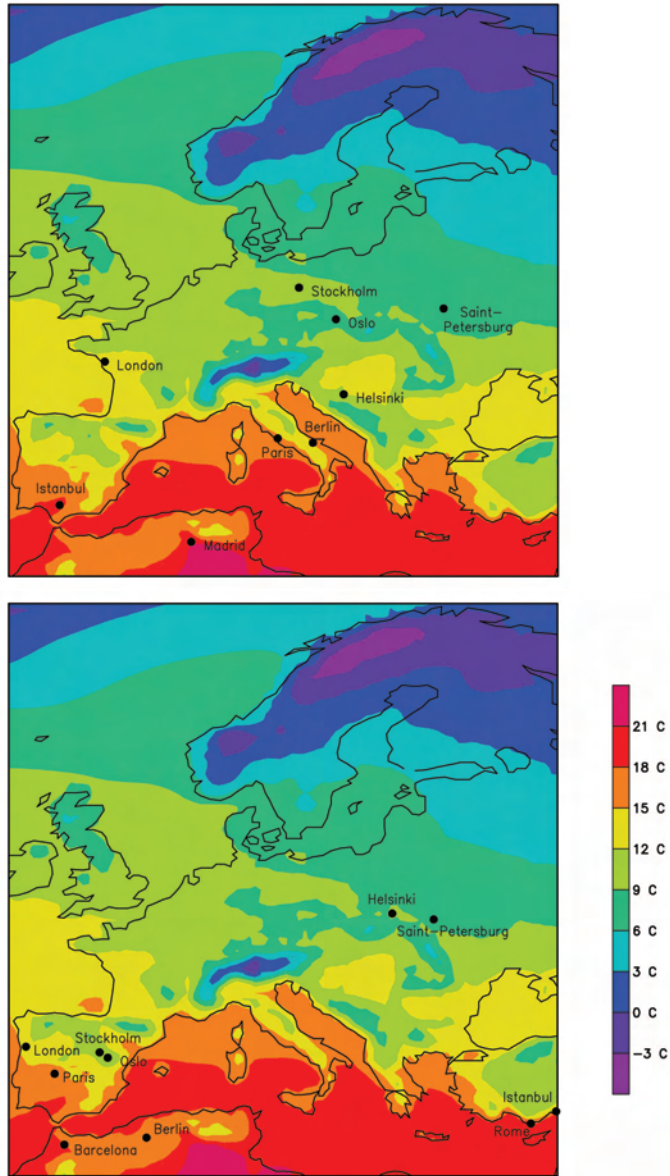


Figure 8: Relocation of European climates at the end of the 21st century, analogues found with the datasets coming from the ARPEGE (left) and the HadRM3H (right) model runs in an A2 global warming scenario. Both are displayed on a mean temperature background from the HadRM3H control run (1961-1990) for easier visual comparison and a basic impression of relative temperatures.

Using two datasets, analogues for 12 European cities were computed: Athens, Barcelona, Berlin, Helsinki, Istanbul, London, Madrid, Oslo, Paris, Rome, Saint-Petersburg and Stockholm. Two climate simulation models projecting different degrees of global warming for the A2 emissions scenario were used: The ARPEGE model from CNRM/Météo-France and the HadRM3H model from the Hadley Center. Both show a clear drift in climate relocation towards warmer regions for Europe.

The analogues of Paris are representative of the kind of scientific policy-oriented message this method provides: according to one simulation, Paris could have at the end of the 21st century a climate similar to Vieste Aero near Rome. That may not be seen as an adverse change by many stakeholders. However, according to another simulation, Paris could also have the climate of the city of Badajoz in Southern Spain. It is widely held that heat waves and water shortages, which were not considered as a significant problem in Paris only ten years ago, are nowadays recurring sources of trouble in the Badajoz area. This work illustrates, therefore, how new climate-related problems will appear in numerous cities because of climate change. The related evolution of natural risks has to be managed in the most proactive ways to avoid the repetition of costly surprises like the 2003 heat wave in Europe and its dramatic consequences.

In some cases no suitable analogue for the projected climate of a given city were found. This indicates a lack of the type of climate projected for the city within Europe, at a 50% confidence level. For example, Athens lacks a good analogue on Figure 7. It can only be supposed that a suitable analogue might be found further south. An obvious extension of this work would be to search potential analogues not only within Europe but worldwide and to assess sources of uncertainty within a larger range of models and scenarios. Another would be to search for the analogue using climatological observation data instead of model-based datasets.

Evidence of this method's communication value comes from its use in teaching and in European popular science and mass media (Kopf et al., 2007; Hallegatte, 2007; Adam, 2007). In addition to, and in comparison with existing socio-economic simulations (e.g. Lorenzoni et al., 2000; Kaivo-oja et al., 2004) for future scenarios, climate analogues provide an alternative way to rigorously frame the climate change issue on cities, as well as provide an estimate of the extent of uncertainty in the prediction of climatic changes. Although the limitations and drawbacks of this method have to be kept in mind, it provides a strong basis for the visualization of climate change and allows socio-economic adaptation to different climates to enter the mental model.

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Appendix A: Parameterization of the Kolmogorov-Smirnov tests

To determine the p_{value} corresponding to a value of the 2 and 3-dimensional Kolmogorov-Smirnov statistic D , we derived a set of sample probability distributions from the procedure and data reported in Appendix A and B of Fasano and Franceschini (1987), and calculated the appropriate approximation formulae for each needed sample size (and a variety of correlation coefficients) through third order polynomial interpolations using an appropriate function from Press et al. (1986). In the 2-dimensional case, data points of the probability distribution for the needed sample sizes were calculated using the polynomial expansion proposed by Fasano and Franceschini (1987) for the 2-dimensional Kolmogorov-Smirnov test. In the 3-dimensional case, the data points for the needed sample sizes were obtained by linear interpolation of the data calculated by Fasano and Franceschini (1987) with Monte Carlo simulations. The range of correlation coefficients covered (in both the 2 and 3-dimensional case) were $CC=0, 0.5, 0.6, 0.7, 0.8$ and 0.9 as values between 0 and 0.5 do not differ significantly from the uncorrelated $CC = 0$ case. As our calculations with the three climate indicators Aridity Index, HDD and CDD in the 3-dimensional test did not yield partial correlation coefficients exceeding 0.95 , the average $\bar{\rho}$ of the $3 CC$ could be used (Fasano and Franceschini, 1987). Table 1 and 2 report the constants of the derived polynomials for the 2 and 3-dimensional case of the main scenario of sample distributions with 30 samples (i.e. annual Aridity Index and Degree Days over 30 years). Sample points and polynomial estimates for the main scenario are furthermore visualized in Figure 9 and 10. All polynomials have the form:

$$p_{value}(d) = \begin{cases} 1.0 & \text{if } d < d_{\min} \\ c_1 d^3 + c_2 d^2 + c_3 d + c_4 & \text{if } d \in [d_{\min}; d_{\max}] \\ 0.0 & \text{if } d > d_{\max} \end{cases} \quad (12)$$

Table 1: Polynomial constants of the probability distribution approximation for the 2-dimensional case

CC	d_{\min}	d_{\max}	c_1	c_2	c_3	c_4
0.0	0.222	0.462	-32.134	52.213	-27.686	4.825
0.5	0.219	0.459	-32.138	51.894	-27.336	4.733
0.6	0.216	0.457	-29.879	49.164	-26.191	4.563
0.7	0.211	0.454	-29.759	48.448	-25.569	4.417
0.8	0.202	0.448	-30.900	48.514	-24.890	4.202
0.9	0.185	0.436	-31.123	46.797	-23.101	3.766

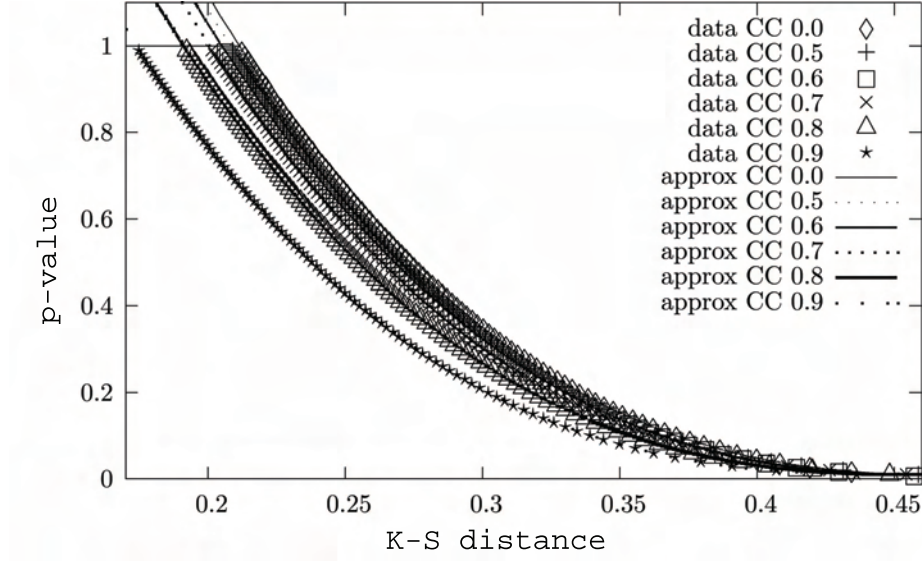


Figure 9: Sample points and polynomial estimates of the probability distribution for the 2-dimensional case

Table 2: Polynomial constants of the probability distribution approximation for the 3-dimensional case

CC	d_{\min}	d_{\max}	c_1	c_2	c_3	c_4
0.0	0.234	0.468	-26.314	49.131	-28.606	5.334
0.5	0.225	0.467	-37.054	59.458	-31.334	5.450
0.6	0.220	0.464	-35.685	57.477	-30.257	5.240
0.7	0.211	0.458	-36.224	56.879	-29.311	4.984
0.8	0.203	0.454	-49.571	69.975	-33.069	5.239
0.9	0.190	0.443	-56.376	74.752	-33.367	5.023

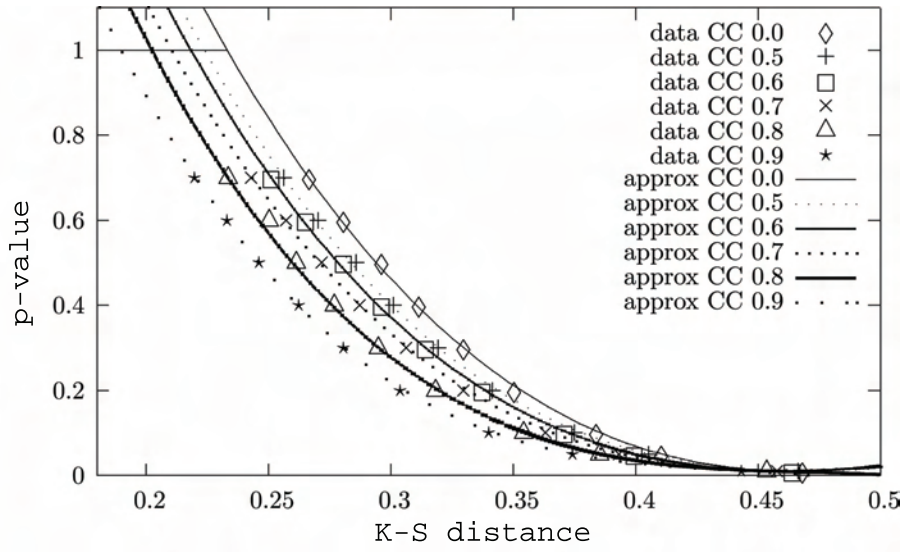


Figure 10: Sample points and polynomial estimates of the probability distribution for the 3-dimensional case

Appendix B: Comparing three versus two climate indicators

We compared the results obtained using a 3-dimensional Kolmogorov-Smirnov test on the 3 climate indicators Aridity Index, Heating Degree Days and Cooling Degree Days with results obtained using only a 2-dimensional test on Aridity Index plus either kind of Degree Days. Table 3, in any cell the ζ mini barchart (the three black rectangular bars) allows to compare the p -value of same location using the three different tests. The table shows that for the 12 European cities examined in this study, results are as expected:

- Analogues found with the three indicators are not as good as analogues found with only two indicators, in absolute terms. For example, Stockholm has an excellent match ($p \approx 100\%$) with either (AI,CDD) or (AI,HDD), but only a good match (61%) with the complete set of criteria.
- Analogues found with the complete set of 3 criteria, in the first column, are also good analogues when tested with only two criteria. In the leftmost column, all 3 bars in the mini barcharts are generally high. This shows the good performance of the locations found by the 3-indicators test for all three testing methods.
- The converse is not true. In the middle and right column, it is generally the case that only the bar of the maximized criteria is good. This means that the climate analogue would be rejected when tested with any of the two other set of indicators.

The results indicate that optimal analogues found using only two indicators are bad when the third climate indicator is considered. Analogues with three indicators are more robust, which supports our choice to use three climate indicators instead of only two.

Table 3: Robustness of analogues computed with 3 indicators (HadRM3H dataset). In each cell, the mini barchart shows the climatic similarity between the station named in that cell and the city indicated in column 1, for three different ways to define climatic similarity. The three different ways to define climatic similarity are: using all three climate indicators (left bar), using only aridity and HDD (middle bar), and using only aridity and CDD (right bar). The station named in each cell is the best analogue for one of the three ways, as indicated by the respective column caption. The vertical scale of the barcharts goes from 0 (—) to 1 (■), each bar representating a p -value, i.e. taller bars in the barcharts indicate more similar climates.

City	City's future best analogue, climates compared on:		
	Aridity, HDD and CDD	Aridity and HDD	Aridity and CDD
Athens	no good analogue	■ El Arfiane	—■ Ghardaia
Barcelona	■ Ouezzane	■ Tunis/Carthage	—■ Bordj Bou Arrer
Berlin	■ Chlef	■ Cahors	—■ Sremska Mitrovi
Helsinki	■ Sandomierz	■ Przemysl	—■ Tours
Istanbul	■ Karaman	■ Laghouat	—■ Laghouat
London	■ Vila Real	■ Ciudad-Real	—■ Lubny
Madrid	no good analogue	■ Geryville	—■ El Aliod
Oslo	■ Teruel	■ Iasi	—■ Zlynka
Paris	■ Badajoz	■ Kumkoy	—■ Ciudad-Real
Rome	■ Nicosia	■ Sagres	—■ Djelfa
Saint-Petersburg	■ Ternopol	■ Siedlce	—■ Sandomierz
Stockholm	■ Soria	■ Oradea	—■ Zlynka

Appendix C: Displaying K-S statistic D instead of the p -value

For visualization of the Kolmogorov Smirnov test results, we have chosen to display the K-S statistic D rather than the corresponding p_{value} . The relationship between D and p is obviously monotonous, so mathematically no information is lost, and the selection does not affect the location of the optimum analogue.

Figure 11 illustrates the difference between a D map and a p map. Admittedly, displaying p -values would be more meaningful to the statistician theoretically. But to everyone else, the K-S statistic gives a better visual indication of graduated differences between climates. This is because, as 4 shows, the $p(D)$ function is very nonlinear. Lower values of D give practically $p = 1$, and higher values give $p = 0$. Therefore, displaying p on a linear scale tends to produce more categorical maps of “good” versus “poor” analogues, while displaying D produce more gradual, esthetically pleasing maps. Figure 12 shows the 3-dimensional K-S statistic for all 12 examined cities (HadRM3H model simulation).

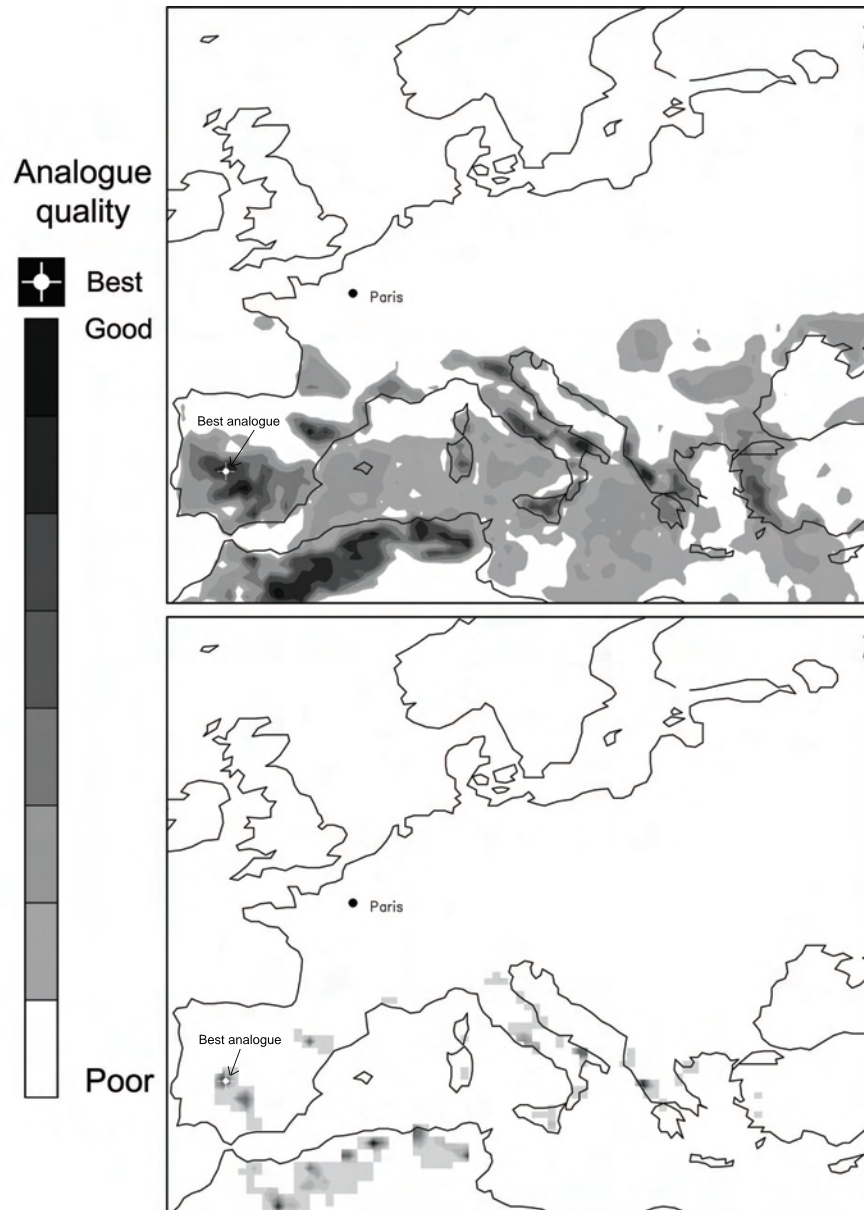


Figure 11: Comparing the 3-dimensional K-S statistic D map (top) with the probabilistic p_{value} map (bottom). The later has stronger variation between grid points. HadRM3H model simulation.

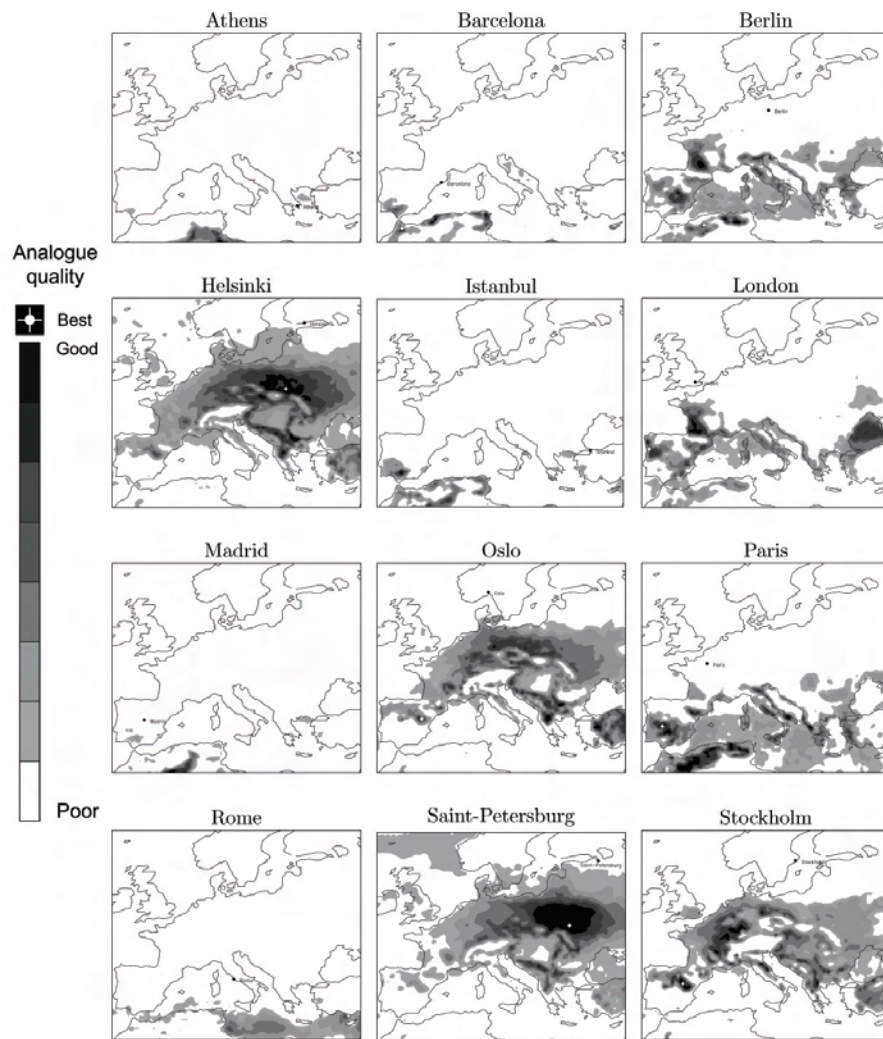


Figure 12: Visualization of the 3-dimensional K-S statistic for all 12 examined cities (HadRM3H model simulation)